Cartogram

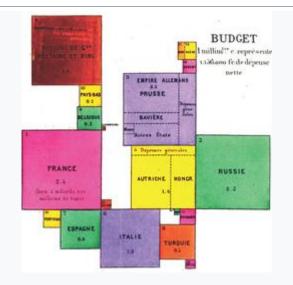


Mosaic cartogram showing the distribution of the global population. Each of the 15,266 pixels represents the home country of 500,000 people – cartogram by Max Roser for Our World in Data

A **cartogram** (also called a **value-area map** or an **anamorphic map**, the latter common among German-speakers) is a thematic map of a set of features (countries, provinces, etc.), in which their geographic size is altered to be directly proportional to a selected ratio-level variable, such as travel time, population, or GNP. Geographic space itself is thus warped, sometimes extremely, in order to visualize the distribution of the variable. It is one of the most abstract types of map; in fact, some forms may more properly be called diagrams. They are primarily used to display emphasis and for analysis as nomographs.^[1]

Cartograms leverage the fact that size is the most intuitive visual variable for representing a total amount.^[2] In this, it is a strategy that is similar to proportional symbol maps, which scale point features, and many flow maps, which scale the weight of linear features. However, these two techniques only scale the map symbol, not space itself; a map that stretches the length of linear features is considered a linear cartogram (although additional flow map techniques may be added). Once constructed, cartograms are often used as a base for other thematic mapping techniques to visualize additional variables, such as choropleth mapping.

History



One of Levasseur's 1876 cartograms of Europe, the earliest known published example of this technique.

The cartogram was developed later than other types of thematic maps, but followed the same tradition of innovation in France.^[3] The earliest known cartogram was published in 1876 by French statistician and geographer Pierre Émile Levasseur, who created a series of maps that represented the countries of Europe as squares, sized according to a variable and arranged in their general geographical position (with separate maps scaled by area, population, religious adherents, and national budget).^[4] Later reviewers have called his figures a statistical diagram rather than a map, but Levasseur referred to it as a carte figurative, the common term then in use for any thematic map. He produced them as teaching aids, immediately recognizing the intuitive power of size as a visual variable: "It is impossible that the child is not struck by the importance of the trade of Western Europe in relation to that of Eastern Europe, that he does not notice how much England, which has a small territory but outweighs other nations by its wealth and especially by its navy, how much on the contrary Russia which, by its area and its population occupies the first rank, is still left behind by other nations in the commerce and navigation."

Levasseur's technique does not appear to have been adopted by others, and relatively few similar maps appear for many years. The next notable development was a pair of maps by <u>Hermann Haack</u> and Hugo Weichel of the <u>1898 election results</u> for the <u>German Reichstag</u> in preparation for the <u>1903 election</u>, the earliest known *contiguous cartogram*.^[5] Both maps

showed a similar outline of the German Empire, with one subdivided into constituencies to scale, and the other distorting the constituencies by area. The subsequent expansion of densely populated areas around <u>Berlin</u>, <u>Hamburg</u>, and <u>Saxony</u> was intended to visualize the controversial tendency of the mainly urban <u>Social Democrats</u> to win the popular vote, while the mainly rural <u>Zentrum</u> won more seats (thus presaging the modern popularity of cartograms for showing the same tendencies in recent elections in the United States).^[6]

The continuous cartogram emerged soon after in the United States, where a variety appeared in the popular media after 1911.^{[7][8]} Most were rather crudely drawn compared to Haack and Weichel, with the exception of the "rectangular statistical cartograms" by the American master cartographer <u>Erwin Raisz</u>, who claimed to have invented the technique.^{[9][10]}

When Haack and Weichel referred to their map as a *kartogramm*, this term was commonly being used to refer to all thematic maps, especially in Europe.^{[11][12]} It was not until Raisz and other academic cartographers stated their preference for a restricted use of the term in their textbooks (Raisz initially espousing *value-area cartogram*) that the current meaning was gradually adopted.^{[13][14]}

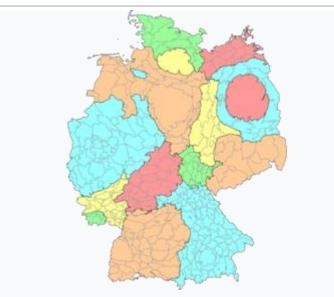
The primary challenge of cartograms has always been the drafting of the distorted shapes, making them a prime target for computer automation. <u>Waldo R. Tobler</u> developed one of the first algorithms in 1963, based on a strategy of warping space itself rather than the distinct districts.^[15] Since then, a wide variety of algorithms have been developed (see below), although it is still common to craft cartograms manually.^[1]

General principles

Since the early days of the academic study of cartograms, they have been compared to <u>map projections</u> in many ways, in that both methods transform (and thus distort) space itself.^[15] The goal of designing a cartogram or a map projection is therefore to represent one or more aspects of geographic phenomena as accurately as possible, while minimizing the collateral damage of distortion in other aspects. In the case of cartograms, by scaling features to have a size proportional to a variable other than their actual size, the danger is that the features will be distorted to the degree that they are no longer recognizable to map readers, making them less useful.

As with map projections, the tradeoffs inherent in cartograms have led to a wide variety of strategies, including manual methods and dozens of computer algorithms that produce very different results from the same source data. The quality of each type of cartogram is typically judged on how accurately it scales each feature, as well as on how (and how well) it attempts to preserve some form of recognizability in the features, usually in two aspects: <u>shape</u> and <u>topological relationship</u> (i.e., retained adjacency of neighboring features).^{[16][17]} It is likely impossible to preserve both of these, so some cartogram methods attempt to preserve one at the expense of the other, some attempt a compromise solution of balancing the distortion of both, and other methods do not attempt to preserve either one, sacrificing all recognizability to achieve another goal.

Area cartograms



Cartogram of <u>Germany</u>, with the states and districts resized according to population

The area cartogram is by far the most common form; it scales a set of region features, usually administrative districts such as counties or countries, such that the <u>area</u> of each district is <u>directly proportional</u> to a given variable. Usually this variable represents the total count or amount of something, such as total <u>Population</u>, <u>Gross domestic product</u>, or the number of retail outlets of a given brand or type. Other strictly

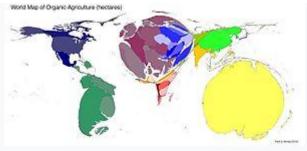
positive <u>ratio</u> variables can also be used, such as <u>GDP per</u> <u>capita</u> or <u>Birth rate</u>, but these can sometimes produce misleading results because of the natural tendency to interpret size as total amount.^[2] Of these, total population is probably the most common variable, sometimes called an *isodemographic map*.

The various strategies and algorithms have been classified a number of ways, generally according to their strategies with respect to preserving shape and topology. Those that preserve shape are sometimes called *equiform*, although *isomorphic* (same-shape) or *homomorphic* (similar-shape) may be better terms. Three broad categories are widely accepted: contiguous (preserve topology, distort shape), non-contiguous (preserve shape, distort topology), and diagrammatic (distort both). Recently, more thorough taxonomies by Nusrat and Kobourov, Markowska, and others have built on this basic framework in an attempt to capture the variety in approaches that have been proposed and in the appearances of the results.^{[18][19]} The various taxonomies tend to agree on the following general types of area cartograms.

Anamorphic Projection

This is a type of contiguous cartogram that uses a single parametric mathematical formula (such as a polynomial curved surface) to distort space itself to equalize the spatial distribution of the chosen variable, rather than distorting the individual features. Because of this distinction, preferred call the some have to result a pseudocartogram.^[20] Tobler's first computer cartogram algorithm was based on this strategy,^{[15][21]} for which he developed the general mathematical construct on which his and subsequent algorithms are based.^[15] This approach first models the distribution of the chosen variable as a continuous density function (usually using a least squares fitting), then uses the inverse of that function to adjust the space such that the density is equalized. The Gastner-Newman algorithm, one of the most popular tools used today, is a more advanced version of this approach.[22][23] Because they do not directly scale the districts, there is no guarantee that the area of each district is exactly equal to its value.

Shape-warping contiguous cartograms



Contiguous cartogram (Gastner-Newman) of the world with each country rescaled in proportion to the hectares of certified <u>organic farming^[24]</u>

Also called *irregular cartograms* or *deformation cartograms*,^[19] This is a family of very different algorithms that scale and deform the shape of each district while maintaining adjacent edges. This approach has its roots in the early 20th Century cartograms of Haack and Weichel and others, although these were rarely as mathematically precise as current computerized versions. The variety of approaches that have been proposed include <u>cellular automata</u>, <u>quadtree partitions</u>, <u>cartographic generalization</u>, <u>medial axes</u>, spring-like forces, and simulations of inflation and deflation.^[18] Some attempt to preserve some semblance of the original shape (and may thus be termed *homomorphic*),^[25] but these are often more complex and slower algorithms than those that severely distort shape.

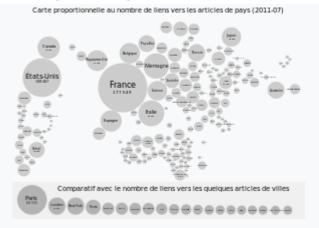
Non-contiguous isomorphic cartograms



Non-contiguous isomorphic cartogram of the <u>Czech Republic</u>, in which the size of each district is proportional to the Catholic percentage and the color (choropleth) representing the proportion voting for the KDU-CSL party in 2010, showing a strong correlation.

This is perhaps the simplest method for constructing a cartogram, in which each district is simply reduced or enlarged in size according to the variable without altering its shape at all.^[16] In most cases, a second step adjusts the location of each shape to reduce gaps and overlaps between the shapes, but their boundaries are not actually adjacent. While the

preservation of shape is a prime advantage of this approach, the results often have a haphazard appearance because the individual districts do not fit together well.



Diagrammatic (Dorling) cartograms[edit]

Diagrammatic (Dorling) cartogram of the number of times each country is linked in the French-language Wikipedia.

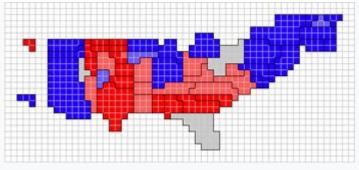
In this approach, each district is replaced with a simple geometric shape of proportional size. Thus, the original shape is completely eliminated, and contiguity may be retained in a limited form or not at all. Although they are usually referred to as *Dorling cartograms* after Daniel Dorling's 1996 algorithm first facilitated their construction,^[26] these are actually the original form of cartogram, dating back to Levasseur (1876)^[4] and Raisz (1934).^[9] Several options are available for the geometric shapes:

- Circles (Dorling), typically brought together to be touching and arranged to retain some semblance of the overall shape of the original space.^[26] These often look like <u>proportional symbol maps</u>, and some consider them to be a hybrid between the two types of thematic map.
- **Squares** (Levasseur/Demers), treated in much the same way as the circles, although they do not generally fit together as simply.
- **Rectangles** (Raisz), in which the height and width of each rectangular district is adjusted to fit within an overall shape. The result looks much like a <u>treemap diagram</u>, although the latter is generally sorted by size rather than geography. These are often contiguous, although the contiguity may be illusory because many of the districts

that are adjacent in the map may not be the same as those that are adjacent in reality.

Because the districts are not at all recognizable, this approach is most useful and popular for situations in which the shapes would not be familiar to map readers anyway (e.g., <u>U.K. parliamentary constituencies</u>) or where the districts are so familiar to map readers that their general distribution is sufficient information to recognize them (e.g., countries of the world). Typically, this method is used when it is more important for readers to ascertain the overall geographic pattern than to identify particular districts; if identification is needed, the individual geometric shapes are often labeled.

Mosaic cartograms



Mosaic cartogram of United States Electoral College results (scaled by 2008 electors) of four past Presidential elections (1996, 2000, 2004, 2008)

States carried by the Republican in all four elections

States carried by the Republican in three of the four elections

States carried by each party twice in the four elections

States carried by the Democrat in three of the four elections

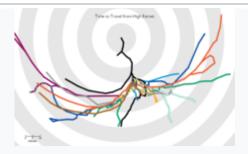
States carried by the Democrat in all four elections

In this approach (also called *block* or *regular cartograms*), each shape is not just scaled or warped, but is reconstructed from a discrete <u>tessellation</u> of space, usually into squares or hexagons. Each cell of the tessellation represents a constant value of the variable (e.g., 5000 residents), so the number of whole cells to be occupied can be calculated (although rounding error often means that the final area is not exactly proportional to the variable). Then a shape is assembled from those cells, usually with some attempt to retain the original shape, including salient features such as panhandles that aid recognition (for example, <u>Long Island</u> and <u>Cape Cod</u> are often exaggerated). Thus, these cartograms are usually homomorphic and at least partially contiguous.

This method works best with variables that are already measured as a relatively low-valued integer, enabling a one-to-one match with the cells. This has made them very popular for visualizing the United States Electoral College that determines the election of the president. appearing on television coverage and numerous vote-tracking websites.^[27] Several examples of block cartograms were published during the 2016 U.S. presidential election season by The Washington Post,^[28] the Five Thirty Eight blog,^[29] and the Wall Street Journal,^[30] among others.

The major disadvantage of this type of cartogram has traditionally been that they had to be constructed manually, but recently algorithms have been developed to automatically generate both square and hexagonal mosaic cartograms.^{[31][32]} One of these, Tilegrams, even admits that the results of their algorithm is not perfect and provides a way for users to edit the product.

Linear cartograms



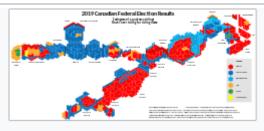
A linear cartogram of the London Underground, with distance distorted to represent travel time from High Barnet station

While an area cartogram manipulates the area of a polygon feature, a **linear cartogram** manipulates linear distance on a line feature. The spatial distortion allows the map reader to easily visualize intangible concepts such as travel time and connectivity on a network. Distance cartograms are also useful for comparing such concepts among different geographic features. A distance cartogram may also be called a *central-point cartogram*.

A common use of distance cartograms is to show the relative travel times and directions from vertices in a network. For example, on a distance cartogram showing travel time between cities, the less time required to get from one city to another, the shorter the distance on the cartogram will be. When it takes a longer time to travel between two cities, they will be shown as further apart in the cartogram, even if they are physically close together.

Distance cartograms are also used to show connectivity. This is common on subway and metro maps, where stations and stops are shown as being the same distance apart on the map even though the true distance varies. Though the exact time and distance from one location to another is distorted, these cartograms are still useful for travel and analysis.

Multivariate cartograms



Hexagonal mosaic cartogram of the results of the 2019 Canadian parliamentary election, colored with the party of each winner using a nominal choropleth technique.

Both area and linear cartograms adjust the base geometry of the map, but neither has any requirements for how each feature is symbolized. This means that symbology can be used to represent a second variable using a different type of thematic mapping technique.^[16] For linear cartograms, line width can be scaled as a flow map to represent a variable such as traffic volume. For area cartograms, it is very common to fill each district with a color as a choropleth map. For example, WorldMapper has used this technique to map topics relating to global social issues, such as poverty or malnutrition; a cartogram based on total population is combined with a choropleth of a socioeconomic variable, giving readers a clear visualization of the number of people living in underprivileged conditions.

Another option for diagrammatic cartograms is to subdivide the shapes as charts (commonly a <u>pie chart</u>), in the same fashion often done with <u>proportional symbol maps</u>. This can be very effective for showing complex variables such as population composition, but can be overwhelming if there are a large number of symbols or if the individual symbols are very small.

Production

One of the first cartographers to generate cartograms with the aid of computer visualization was <u>Waldo Tobler</u> of <u>UC Santa Barbara</u> in the 1960s. Prior to Tobler's work, cartograms were created by hand (as they occasionally still are). The <u>National Center for Geographic Information</u> and <u>Analysis</u> located on the UCSB campus maintains an online <u>Cartogram Central</u> with resources regarding cartograms.

A number of software packages generate cartograms. Most of the available cartogram generation tools work in conjunction with other GIS software tools as add-ons or independently produce cartographic outputs from GIS data formatted to work with commonly used GIS products. Examples of cartogram software include ScapeToad,^{[33][34]} Cart,^[35] and the Cartogram Processing Tool (an ArcScript for ESRI's ArcGIS), which all use the Gastner-Newman algorithm.^{[36][37]} An alternative algorithm, Carto3F,^[38] is also implemented as an independent program for non-commercial use on Windows platforms.^[39] This program also provides an optimization to the original Dougenik rubber-sheet algorithm.^{[40] [41]} The <u>CRAN</u> package <u>recmap</u> provides an implementation of a rectangular cartogram algorithm.[42]

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